## ПАПIBIA UПIVERSITY of SCIEMCE AMD TECHMOLOGY

FACULTY OF HEALTH, NATURAL RESOURCES AND APPLIED SCIENCES SCHOOL OF NATURAL AND APPLIED SCIENCES

DEPARTMENT OF MATHEMATICS, STATISTICS AND ACTUARIAL SCIENCE

| QUALIFICATION: Bachelor of science ; Bachelor of science in Applied Mathematics and Statistics |  |
| :--- | :--- |
| QUALIFICATION CODE: O7BSAMS | LEVEL: 6 |
| COURSE CODE: FIM601S | COURSE NAME: FINANCIAL MATHEMATICS 2 |
| SESSION: JUNE 2023 | PAPER: THEORY |
| DURATION: 3 HOURS | MARKS: 100 |


| FIRST OPPORTUNITY EXAMINATION QUESTION PAPER |  |
| :--- | :---: |
| EXAMINER | Dr V. Katoma |
|  | Mrs. H.Y Nkalle |
| MODERATOR: | Prof. A.S. Eegunjobi |


| INSTRUCTIONS |
| :--- |
| - Answer ALL the questions in the booklet provided. |
| - Show clearly all the steps used in the calculations. |
| - All written work must be done in blue or black ink and sketches |
| must be done in pencil. |

## PERMISSIBLE MATERIALS

- Non-programmable calculator without a cover.

THIS QUESTION PAPER CONSISTS OF 3 PAGES (Including this front page)
Question 1[25]
1.1 Define the following terms
1.1.1 Net Present Value ..... [2]
1.1.2 Internal Rate of Return ..... [2]
1.1.3 Discounted Cash flow ..... [2]
1.1.4 Zero-coupon bond ..... [2]
1.2 Name four (4) Instruments in the money markets. ..... [4]
1.3 Explain three (3) ways in which Derivatives can be used.[6]
1.4 VK Investment cc has an existing debt of $N \$ 2,000000$ on which it makes annual payments at an annual effective rate of LIBOR plus $0.5 \%$. VK Investment cc decides to enter a swap with a notional amount of $N \$ 2000000$ on which it makes annual payments at a fixed annual effective rate of $3 \%$ in exchange for receiving annual payments at the annual effective LIBOR rate. The annual effective LIBOR rates over the first and second years of the swap contract are $2.5 \%$ and $4 \%$ respectively. VK Investment cc does not make or receive any other payments. Calculate the net interest payment that VK Investment cc makes in the second year.

## Question 2 [25]

2.1 Explain the difference between a Forward and Future contract
2.2 An investment of $N \$ 200.00$ returns $N \$ 120.00$ at the end of $1^{\text {st }}$ year and $N \$ 100.00$ at the end of $2^{\text {nd }}$ year. What is the internal rate of return (IRR)?
2.3 Consider a $3 \times 9$ FRA for $£ 1,000,000$ with an FRA rate of $3.4 \%$. Suppose the reference rate is LIBOR and the 6 -month LIBOR on the effective date is $3.7 \%$. Assume ACT/360 and the loan is for a period of 180 days. Find how much the borrower receives from the lender on the effective date.
2.4 Yvonne is considering a project which requires an amount of $N \$ 3000.00$ and another amount of $N \$ 1000.00$ after one year. In two years', time, when the project ends, she expects an inflow of $N \$ 4500.00$. Assume that Yvonne can lend and borrow at the same fixed rate of $7.13 \%$ per annum.
2.4.1 what is the internal rate of return (IRR) of this project?

## Question 3 [25]

3.1 Consider the following two cash-flow sequence:

| Time (Year) | 0 | 1 | 2 | 3 |
| :--- | :--- | :--- | :--- | :--- |
| Project A | -80 | 96 | 1 | 5 |
| Project B | -80 | 10 | 10 | 90 |

Show that $N P V(A)>N P V(B)$ if the interest rate is $r=0.06$ or $6 \%$.
3.2 Why would you prefer the given interest rate $i$ to be less than the internal rate of return (IRR) for the investment to be viable
3.4 An investor is considering whether to invest in either of the following loans:

Loan A: For a purchase price of N\$20000, the investor will receive N\$ 1000 per annum payable quarterly in arrear for 15 years.
Loan B: For a purchase price $N \$ 11000$, the investor will receive an income of $N \$ 605$ per annum, payable annually in arrear for 18 years, and a return of his outlay at the end of this period. The investor may borrow money at 4\% per annum. Which Loan is more profitable to invest in?

## Question 4 [25]

4.1 Suppose a CD is issued with a face value of $£ 500,000$ and a coupon of $6 \%$ for 90 days. (a) After 30 days, its yield has fallen to $5.75 \%$. What is its price? (b) After a further 30 days its yield has risen back to $6 \%$. What is the rate of return for holding this CD for the 30 days: day 30 to day 60. (Assume ACT/365.)
4.2 A loan is being repaid by 10 equal annual payments of $\mathrm{N} \$ 400$. Suppose the effective annual interest rate is $12 \%$. Find the loan outstanding immediately after the payment at the end of year six (6).
4.3 Suppose A borrows $£ 1,000$ for 3 years at an effective interest rate of $7 \%$ per annum. Suppose further that A repays the loan by equal amounts of $x$ at the ends of years 1,2 and 3 .

### 4.3.1 Find $x$

4.3.2 Derive a loan schedule for this amortization

